# Mechanism of the Vanadium Oxide-Catalyzed Selective Reduction of NO by NH<sub>3</sub>. A Quantum Chemical Modeling

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Quantum chemical calculations have been performed using density functional theory to model the mechanism of selective catalytic reduction of NO by  $NH_3$  on vanadium oxide. The reaction is initiated by  $NH_3$  adsorption on a Brønsted site modeled as a dimer cluster model representative of vanadium oxide, containing a terminal V=O adjacent to a V-OH group. The calculations indicate that the adsorbed  $NH_3$  behaves as  $NH_4^+$ , which is supported by calculated IR spectra. Subsequently NO reacts with this activated  $NH_3$  to yield  $NH_2NO$  and finally the reaction products  $N_2$  and  $H_2O$ . The present results give support to a dual-site Eley-Rideal-type mechanism involving a Brønsted site and agree with isotopic labeling studies.

### I. Introduction

Because of its environmental importance, the selective catalytic reduction (SCR) of  $NO_x$  by  $NH_3$  has been extensively studied. Important features of the reaction have been summarized in reviews.<sup>1</sup> Among the various catalysts which are active in SCR of NO, vanadia-based catalysts are most widely applied due to their excellent activity, selectivity, and stability. Most of the industrial SCR catalysts contain the active vanadia dispersed on TiO<sub>2</sub>, which proved to be the most suitable single oxide support material. Additional components used are SiO<sub>2</sub> for structural promotion and WO<sub>3</sub> for broadening the temperature range for reaction. In this light it is not surprising that most experimental studies on the reaction mechanism have been carried out either on titania-supported vanadia or on pure, unsupported vanadia catalysts. Different reaction mechanisms have been proposed and discussed in the literature.<sup>1–11</sup> Both the reaction mechanisms and the nature of the active vanadia sites are still debated.

It is generally accepted that the vanadium-catalyzed SCR of NO proceeds according to the following stoichiometry:

$$4NO + 4NH_3 + O_2 \rightarrow 4N_2 + 6H_2O$$

Several studies <sup>2,3,9,12,13</sup> revealed that ammonia adsorbs on both Brønsted acid sites (associated with V–OH surface groups) and Lewis acid sites (coordinated form) on vanadia–titania catalysts, which gave rise to different suggestions concerning the reaction mechanism. Based on IR spectroscopic studies, Takagi *et al.*<sup>2,14</sup> proposed a Langmuir–Hinshelwood-type mechanism involving NO, adsorbed as NO<sub>2</sub> (O<sub>s</sub> + NO), and NH<sub>3</sub> adsorbed as NH<sub>4</sub><sup>+</sup>. In contrast, Inomata *et al.*<sup>3</sup> deduced from gas chromatographic (GC) and IR spectroscopic investigations that NH<sub>4</sub><sup>+</sup> acts as the active ammonia species and reacts with gas phase NO according to an Eley–Rideal-type mechanism (ERM). Janssen *et al.*<sup>15</sup> further supported this mechanism by isotopic transient studies involving <sup>18</sup>O<sub>2</sub> and <sup>15</sup>N<sub>2</sub>, which indicated that ammonia does not react with O<sub>2</sub> or O from any source during the reaction; nitrogen and nitrous oxide are produced by a reaction involving all three species: NO, NH<sub>3</sub>, and/or O<sub>2</sub>. Furthermore, it has been shown that, among the NH<sub>3</sub> and NO reactants, only NH<sub>3</sub> is strongly adsorbed.<sup>16</sup> Gasior *et al.*<sup>4</sup> concluded from both IR and XPS measurements on single-crystal surfaces of V<sub>2</sub>O<sub>5</sub> that the SCR proceeds via participation of ammonia adsorbed on Brønsted acid sites. The important role of Brønsted acid sites in SCR of NO has been confirmed recently by in situ FTIR studies on titania-supported vanadia.<sup>17–19</sup> Odriozola *et al.*<sup>6</sup> showed by means of Auger electron spectroscopy and thermal desorption spectroscopy that NO adsorbs only on titania and on reduced vanadia, but not on oxidized vanadia surfaces. A similar behavior was found using positron-emitting <sup>13</sup>NO in SCR.<sup>20</sup>

According to Ramis *et al.*,<sup>13</sup> the reaction proceeds via ammonia adsorbed on Lewis sites of vanadia. This mechanism contrasts those described above, where ammonia bound to Brønsted sites was suggested to be crucial.

Although considerable experimental evidence is available concerning the initial step (ammonia adsorption) of SCR, the subsequent steps have not been clearly elucidated experimentally so far. Theoretical studies of the thermal deNO<sub>x</sub> process<sup>21–28</sup> suggest the reaction of NH<sub>2</sub> with NO to be a primary product channel leading to N<sub>2</sub> and H<sub>2</sub>O, where NH<sub>2</sub>NO has been considered to be a crucial intermediate. The secondary products from this channel seem to be N<sub>2</sub>H + OH,<sup>21,23,24,28</sup> which act as the chain-branching step allowing the process to proceed.<sup>23,24,29–32</sup>

The objective of the present study is to elucidate the role of the  $NH_2 + NO$  interaction in the heterogeneously catalyzed SCR process. This aim has been brought about by means of a density functional theory (DFT) investigation with special focus on (i) the reaction involving an activated  $NH_3^{33}$  with an incoming NO and (ii) the potential energy surface of the adduct  $NH_2NO$ .

The finite cluster approximation to an infinite surface of a substrate is widely used in model studies of chemisorption/ desorption processes in heterogeneous catalysis.<sup>34–38</sup> This approach is valid when the adsorbate creates rather short-range perturbation of a substrate, localized mainly on the active site responsible for substrate—adsorbate bonding. Assuming these conditions to prevail, a V<sub>2</sub>O<sub>9</sub>H cluster (see **1** in Figure 1) of *C<sub>s</sub>* symmetry has been taken to model the surface, in which V atoms adjacent to the cluster were substituted by terminal H atoms. As compared to a full treatment of the bulk crystal or to the

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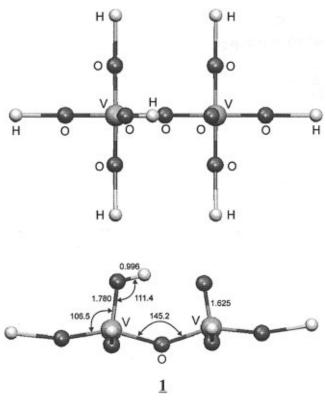


Figure 1.  $V_2O_9H$  cluster 1 used to model the interaction between NH<sub>3</sub> and  $V_2O_5$  surfaces. Distances are in angstroms and angles in degrees.

use of embedded clusters, this approximate treatment can be justified as recently demonstrated by Witko et al.,34 who showed that the electronic structure of the oxygen sites is not changed if the substrate cluster is increased beyond V<sub>2</sub>O<sub>9</sub>H. Further, saturation of the peripheral oxygen bonds by hydrogen has only a minor influence on the oxygen sites.<sup>34,36</sup> In a previous work,<sup>33</sup> we found that DFT calculations were able to reproduce accurately both the V=O and the V-OH bond lengths derived from experimental investigations.<sup>39</sup> We also showed that NH<sub>3</sub> may be adsorbed on V<sub>2</sub>O<sub>5</sub> as a Brønsted-bound ammonia yielding 2a and 2b (Figure 2a,b), in agreement with experimental studies.<sup>2,12,16-18</sup> The chemisorption complex of NH4<sup>+</sup> in 2a has been found to be energetically favored by 14.2 kcal/ mol compared to that in 2b. The adsorption energy of NH<sub>3</sub> on V<sub>2</sub>O<sub>9</sub>H (25.0 kcal/mol) calculated in a previous study<sup>33</sup> agrees well with NH<sub>3</sub> desorption enthalpies derived from temperatureprogrammed desorption measurements (18-26 kcal/mol<sup>19</sup> and 22-28 kcal/mol<sup>40</sup>) carried out over vanadia- and titaniasupported vanadia, suggesting nonactivated ammonia adsorption. Furthermore, we have also evidenced the distorted geometry of the chemisorbed ammonium ion.33

#### **II.** Computational Method

The linear combination of the Gaussian-type orbital-model core potential-density functional theory (LCGTO-MCP-DFT) method<sup>41–44</sup> and its corresponding deMon package<sup>44</sup> has been used. The nonlocal gradient corrections as suggested by Becke<sup>45</sup> for exchange and Perdew<sup>46</sup> for correlation functionals (BP86) have been used in this study. All the core and valence electrons were explicitly taken into account. The one-electron (orbital) basis set used in the calculations has been optimized for LCGTO-MCP-DFT by Godbout *et al.*<sup>47</sup> In our case, the V and H basis sets are of double- $\zeta$  plus polarization quality, and triple- $\zeta$  plus polarization quality, and triple- $\zeta$  plus polarization quality for N and O, the contraction patterns being V(63321/531/41), H(41/1), N(5211/411/1), and O(5211/411/1), which leads in the usual six-component d-type Cartesian Gaussian functions to basis sets of dimension 254 for **1** (Figure

1), 288 for  $1 + NH_3$  (Figure 2a,b), and 326 for  $1 + NH_3 + NO$  (Figure 3). The basis sets required by the LCGTO-DFT model to fit the electron density and the exchange–correlation potential have been chosen as V(5,5;5,5), H(5,1;5,1), N(5,2;5,2), and O(5,2;5,2).

Vibrational analyses were carried out analytically on the optimized structures **1**, **2a**, and **2b** derived from calculations using the Gaussian-94/DFT program package.<sup>48</sup> The 6-31G\* (for H, N, O) and 6-311G\*\* (for V) basis sets were used in these calculations. The starting geometry of the various species used to model the deNO<sub>x</sub> process<sup>33</sup> has been taken from previous calculations performed with the deMon package. The structural parameters of the six coplanar O–H groups bonded to the vanadium atoms have been kept frozen. Each peak of the simulated IR spectra has been assumed to exhibit the shape of a Lorentzian curve in which the width at half-height has been taken equal to 4 cm<sup>-1</sup>.

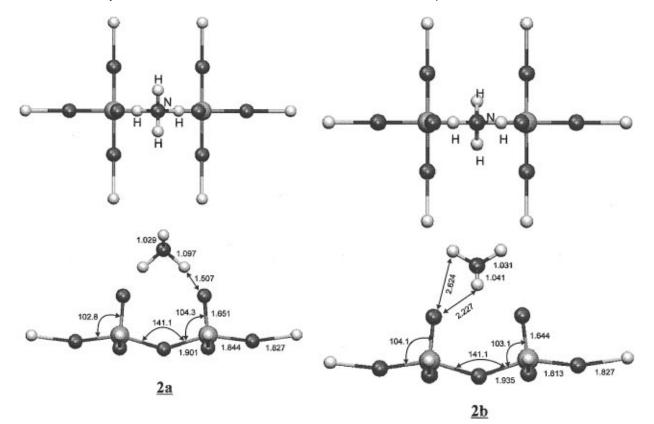
The potential energy surfaces of the initial adduct  $NH_2NO$  and its dissociation reactions have been investigated by using the Gaussian-94/DFT program package.<sup>48</sup> The 6-311++G\*\* basis sets were used for H, N, and O, and extrafine integration grids have been taken in these calculations. The initial geometry of both intermediates and transition states of the relevant reaction steps were extracted from a previous work of Duan and Page.<sup>21</sup> In order to consistently explore the influence of the exchange– correlation functionals have been used: (i) the Becke's<sup>49</sup> three-parameter hybrid method using the Lee, Yang, and Parr correlation functional<sup>50,51</sup> (B3LYP), (ii) the Becke's 1988 exchange functional<sup>45</sup> and the Perdew and Wang's gradient-corrected correlation functional<sup>52</sup> (BPW91), and (iii) the BP86.<sup>45,46</sup>

The calculated harmonic frequencies have been compared with observed frequencies that contain anharmonic contributions. Neither the calculation of anharmonic vibrational energy levels nor experimental determination of harmonic frequencies is routinely practical for polyatomic molecules.<sup>53–55</sup> It requires detailed knowledge of both quadratic and anharmonic force constants, and it is only feasible for very small molecules.

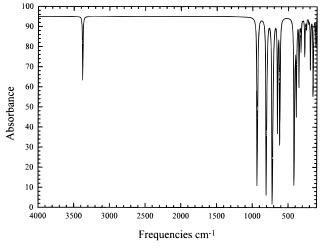
#### **III. Results and Discussion**

The harmonic vibrational frequencies have been calculated analytically for 1, 2a, 2b,  $NH_3$ , and  $NH_4^+$ . Both the ammonia and the ammonium ion were previously optimized at the same level of theory used for 1, 2a, and 2b. The results are listed in Tables 1-4, and the simulated IR spectra are displayed in Figures 3 and 4. Structure 2a exhibits harmonic frequencies that are all positive, whereas 2b has one imaginary frequency (258i cm<sup>-1</sup>), suggesting that **2a** is a local minimum and **2b** a transition state. The simulated IR spectra of 2a, NH<sub>3</sub>, and NH<sub>4</sub><sup>+</sup> have been superimposed in Figure 5. A comparison of these spectra with the in situ IR measured under reaction conditions supports the suggestion that the SCR reaction is initiated by NH<sub>3</sub> adsorption on a Brønsted acid site (V-OH).<sup>17-19</sup> Adsorbed ammonia is then activated by the transfer of H to an adjacent  $V^{5+}=O^{2,12,16-18}$  The present calculations agree with earlier experimental studies,9 which uncovered a direct correlation between the concentration of the Brønsted acid sites and NO conversion, and they are consistent with the observed formation of new reduced V-OH species.9,12

In a subsequent step, efforts toward elucidating the reaction involving 2a and an incoming NO have been undertaken. A plausible initial position of NO has been deduced by sampling the potential energy surface of 3 by performing single-point calculations. The resulting structure 4 is displayed in Figure 6. Then 4 has been optimized by freezing the structural parameters of (i) the oxygen atom bridging the two vanadyl Vanadium Oxide-Catalyzed Selective Reduction



**Figure 2.** (a) NH<sub>3</sub> adsorption on **1**. The activated complex **2a** has a  $C_{2\nu}$  symmetry. Distances are in angstroms and angles in degrees. (b) Alternative NH<sub>3</sub> adsorption on **1**. The transition state **2b** has a  $C_{2\nu}$  symmetry. Distances are in angstroms and angles in degrees.



**Figure 3.** Simulated infrared spectrum of **1**. Each peak of the simulated IR spectra has been assumed to exhibit the shape of a Lorentzian curve in which the width at half-height has been taken equal to  $4 \text{ cm}^{-1}$ .

groups, (ii) the vanadium atoms, and (iii) the six planar O–H groups bonded to the vanadium centers. This led to the release of the adduct H<sub>2</sub>NNO (*N*–nitrosamide) **lm.1** (local minimum) from a V<sup>4+</sup>–OH moiety **5** as shown in Figure 7a,b. The heat of this reaction was found to be equal to +18.2 kcal/mol (+17.0 kcal/mol including the zero-point energies correction), corresponding to an endothermic process. Unfortunately, there are no experimental data of  $\Delta H_0$  for the formation of NH<sub>2</sub>NO reported in the literature.<sup>23</sup> Note that no experimental evidence for the formation of NH<sub>2</sub>NO has been found so far under the SCR conditions. However using a dual-vacuum chamber quadrupole mass spectrometer system Farber and Harris<sup>56</sup> observed NH<sub>2</sub>NO as a major reaction product of the reaction of NH<sub>3</sub> and NO on a vanadium oxide catalyst at 300–400 °C. The formation of NH<sub>2</sub>NO adduct with a minimum lifetime of

TABLE 1: IR Frequencies of the Activated Complex NH<sub>4</sub>V<sub>2</sub>O<sub>3</sub>(OH)<sub>6</sub> 2a Calculated Using the Gaussian-94/DFT Program Package and BP86 Exchange–Correlation Functional

frequency (cm <sup>-1</sup> )	symmetry	intensity	mode description
3495	B1	w	$\nu_{\rm asym}  {\rm N-H_b}^a$
3409	A1	w	$\nu_{\rm sym}$ N–H <sub>b</sub> <sup>a</sup>
2503	A1	vs	$\nu_{\rm sym}  {\rm N-H_a}^b$
2228	B2	W	$\nu_{\rm asym}  {\rm N-H_a}^b$
1663	A1	m	$\delta_{\rm sym}$ N–H
1568	B1	W	$\gamma_{\rm sym}$ N–H
1483	A1	m	$\delta_{\rm asym}$ N–H
1252	B2	W	$\gamma_{\rm sym}$ N–H
915	A1	m	$\delta_{\rm sym}$ V=O
838	B2	vw	$\delta_{asym}$ V=O

<sup>*a*</sup> H pointing away from V=O. <sup>*b*</sup> H pointing to V=O.

TABLE 2: IR Frequencies of the Transition StateNH4V2O3(OH)62b Calculated Using the Gaussian-94/DFTProgram Package and BP86 Exchange–CorrelationFunctional

frequency (cm <sup>-1</sup> )	intensity	frequency (cm <sup>-1</sup> )	intensity
3479	vw	1417	s
3423	w	1365	m
3303	vw	914	s
3272	m	627	m
2134	VS	258i	vw
1428	vw		

100  $\mu s$  was suggested as a primary step in the reaction mechanism leading to  $N_2$  and  $H_2O$  products.^{56}

The V<sup>4+</sup>–OH species can be reoxidized by either NO or O<sub>2</sub> to regenerate V<sup>5+</sup>=O;<sup>9,57</sup> the reaction rate is enhanced in the presence of O<sub>2</sub>.<sup>16</sup> Duffy *et al.*<sup>57</sup> showed that, in the absence of O<sub>2</sub>, reoxidation must be accomplished by nitric oxide. The results of their isotope studies indicate that nitrogen atoms so released end up as ammonia; <sup>15</sup>NH<sub>3</sub> is obtained by using <sup>15</sup>NO as an incoming species. The structural parameters and the corresponding simulated IR spectra of **5** are displayed in Figure

TABLE 3: IR Frequencies of NH<sub>3</sub> Calculated Using the Gaussian-94/DFT Program Package and BP86 Exchange–Correlation Functional

frequency (cm <sup>-1</sup> )	symmetry	intensity	mode description
3468	A1	vw	$\nu_{\rm sym}$ N–H
3332	E	vw	$\nu_{\rm asym}$ N–H
1686	A1	v	$\delta_{d}$ N-H
1116	E	vs	$\delta_{\rm s}$ N–H

TABLE 4: IR Frequencies of  $NH_4^+$  Calculated Using the Gaussian-94/DFT Program Package and BP86 Exchange-Correlation Functional

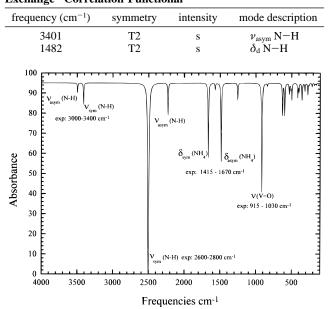


Figure 4. Simulated infrared spectrum of 2a.

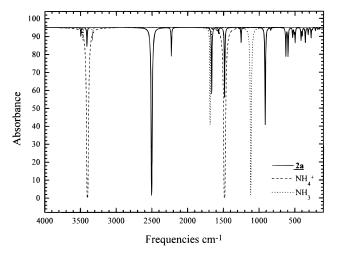


Figure 5. Superposition of simulated infrared spectra of 2a, NH<sub>3</sub>, and NH<sub>4</sub><sup>+</sup>.

7b and Figure 8, respectively. These calculations indicate that (i) **5** is a local minimum (no imaginary frequency exhibited), (ii) neither V–OH<sub>a</sub> nor V–OH<sub>b</sub> exhibits structural or spectroscopic properties similar to those found for the vanadia hydroxyl group in **1**, (iii) H<sub>b</sub> is stabilized by interaction with the lone pair of the oxygen atom bonded to H<sub>a</sub>, (iv) H<sub>a</sub> and H<sub>b</sub> are drastically different, and (v) **5** does not release water spontaneously. The bond lengths differ by 0.062 Å for V–O and 0.028 Å for O–H. The O–H stretching modes  $\nu$ (O–H<sub>a</sub>) and  $\nu$ (O–H<sub>b</sub>) are localized at 3612 and 3105 cm<sup>-1</sup>, respectively, and the corresponding bending modes at 740 and 943 cm<sup>-1</sup>. The new hydroxyl band we calculated at 3612 cm<sup>-1</sup> has also been observed by Topsøe *et al.*<sup>58,59</sup> and R. C. Adams *et al.*<sup>60</sup> around 3650–3700 cm<sup>-1</sup>, through the SCR reaction pathway. It was

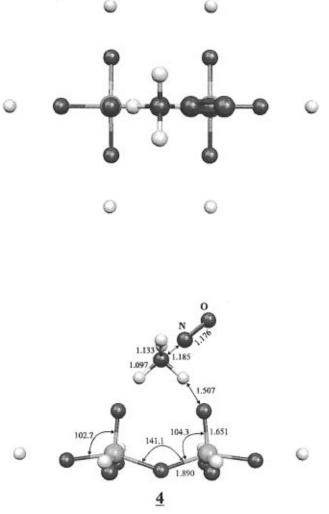


Figure 6. Initial geometry 4 used to model NO reacting with 2a. Distances are in angstroms and valence angles in degrees.

assigned as a hydroxyl on a reduced vanadium center,  $V^{+4}$ -OH, in perfect agreement with the present calculations.

The calculation of the transition state for this reaction turned out to be an intricate task, and no convergence could be achieved using the Gaussian-94/DFT package. However, the barrierless association of NH2 with NO21 prompted us to concentrate on a further aspect of the SCR mechanism. Portions of the potential energy surface of the dissociation reaction of NH<sub>2</sub>NO were characterized by three different gradient corrected methods, i.e. B3LYP, BPW91, and BP86. The results are displayed in Tables 5-8, and the structures of both intermediates and transition states are illustrated in Figure 9. A schematic potential energy diagram of the NH<sub>2</sub>NO dissociation reaction is shown in Figure 10. The qualitative mechanism emerging from these calculations proceeds initially with the association of an adsorbed ammonia with NO to form a highly energized NH<sub>2</sub>NO (lm.1) adduct, which can undergo a 1,3 H atom migration (ts.1), yielding an HNNOH species (Im.2), again with considerable excess internal energy. This species, which has a trans conformation with respect to the NN bond and a cis conformation concerning the NO bond, must isomerize to a cis conformation of the NN bond and a trans conformation (lm.5) of the NO bond before it can undergo a second 1,3 H atom migration, yielding N<sub>2</sub> and H<sub>2</sub>O products. These isomerizations can take place in either order. Isomerization around the NO bond (ts.2) is performed by simple torsional rotation (lm.3), while isomerization around the NN bond (Im.4) occurs by passage through a linear HNN transition state (ts.3). The concerted molecular  $H_2$  elimination from the cis-cis HNNOH complex (**Im.4**) yields Vanadium Oxide-Catalyzed Selective Reduction

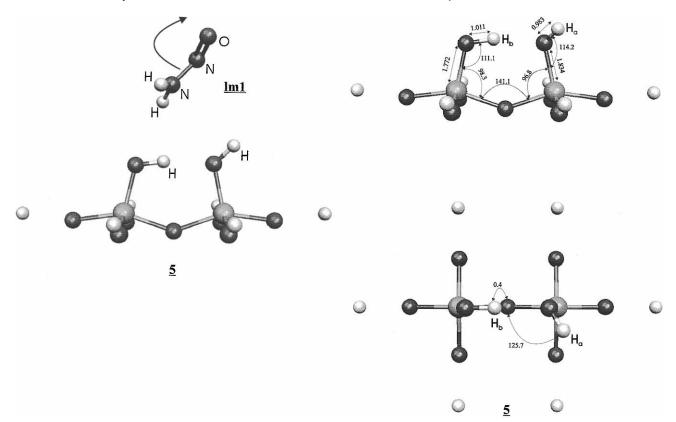


Figure 7. (a, left) Model of the reaction between adsorbed NH<sub>3</sub> with NO, releasing the moiety 5. (b, right) Structure of 5.

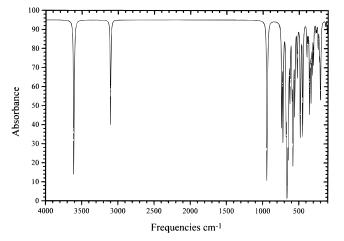


Figure 8. Simulated infrared spectrum of 5.

 $H_2 + N_2O$ . The high activation energy, about 30–40 kcal/mol (Table 7), probably results from the inability of the system to exhibit a linear arrangement of the N2O fragment while keeping the two H atoms in close proximity. The bond lengths derived by the BPW91 and BP86 exchange-correlation functionals are very similar for the stationary points. The absolute mean deviation between the results deduced from these two functionals is about +0.002 Å. On the other hand, the B3LYP functional leads to shorter bond lengths as compared with BPW91. The mean deviations vary from -0.012 Å for  $\delta$ (N–N),  $\delta$ (O–H), and  $\delta(N-H)$  to -0.024 Å for  $\delta(O-N)$ . The same trend is observed for the transition state geometries, but in this case, the mean deviation for  $\delta(O-N)$  is larger (-0.054 Å). The valence bond angles calculated by B3LYP differ significantly from those deduced from BP86 and BPW91 ( $-1.0^{\circ}$ ). The absolute deviation increases to  $2.0^{\circ}$  for  $\alpha(N-N-H)$  for linear HNN transition states (ts.3 and ts.5). The dihedral angles are equivalent whatever exchange-correlation functionals are used.

The relative energies of intermediates and transition states are listed in Table 7. Again, the BPW91 and BP86 functionals lead to similar results with a mean deviation close to 0.5 kcal/ mol. On the other hand, the energy barriers derived by using the B3LYP functional are higher by an amount of 2–5 kcal/ mol. The discrepancy increases to 8 kcal/mol for the energy of the overall reaction NH<sub>2</sub>NO  $\rightarrow$  N<sub>2</sub> + H<sub>2</sub>O.

DF methods yield vibrational frequencies that are consistently closer to experiment than those obtained with the Hartree–Fock (HF) and MP*n* methods. There is an improvement in going from the nonlocal functionals to the hybrid density functional methods.<sup>54,55</sup> The latter lead to harmonic frequencies that are between those calculated with HF (largely overestimated) and MP*n*, and *pure* DF methods.<sup>61–64</sup> The computed harmonic frequencies for the intermediates are displayed in Table 8. The BPW91 and BP86 functionals lead again to similar results for  $\nu$ (NN) and  $\nu$ (NO) but are slightly different for  $\nu$ (NH) and  $\nu$ (OH). The frequencies derived by using the B3LYP functional are higher and drastically different. In this case, the mean deviations vary from 60 cm<sup>-1</sup> for  $\nu$ (NN) and  $\nu$ (NO) to 120 cm<sup>-1</sup> for  $\nu$ (NH) and  $\nu$ (OH) as compared to that estimated by BPW91.

Finally, the mechanism suggested from the above calculations is in accordance with isotopic labeling studies<sup>15,57</sup> and <sup>13</sup>N positron emission,20 which revealed that in SCR over vanadiabased catalysts N<sub>2</sub> is primarily formed by a nitrogen atom originating from nitric oxide and one from ammonia. The relevance of the mechanism studied by considering a dimeric cluster model mimicking the active sites of a vanadium pentoxide surface certainly has its limitations. Although possible influences due to the presence of the support or promotors are not taken into account, comparative catalytic studies performed on titania-supported vanadia and unsupported vanadia revealed a similar catalytic behavior at temperatures up to 350 °C. Thus it seems that the reaction mechanism governing on pure vanadia is also relevant for (titania)-supported vanadia and consequently for the vanadia-based catalysts used in industrial applications.

TABLE 5: Structural Parameters (Å and deg) of Intermediates in the Dissociation Reaction of NH<sub>2</sub>NO Calculated Using the Gaussian-94/DFT Program Package and the B3LYP, PW91, and the BP86 Exchange–Correlation Functionals

	δ- (H−О)	δ- (O-N)	δ- (N-N)	δ- (N-H1)	δ- (N-H2)	α- (H-O-N)	α- (O-N-N)	α- (N-N-H1)	α- (N-N-H2)	α- (H-O-N-N)	α- (O-N-N-H1)	α- (O-N-N-H2)
lm.1		1.222a	1.331 <sup>a</sup>	1.019 <sup>a</sup>	1.009 <sup>a</sup>		114.2 <sup>a</sup>	119.1 <sup>a</sup>	116.9 <sup>a</sup>		$0.1^{a}$	179.9 <sup>a</sup>
		$1.233^{b}$	$1.345^{b}$	$1.027^{b}$	$1.016^{b}$		$114.0^{b}$	$120.3^{b}$	116.9 <sup>b</sup>		$0.1^{b}$	$179.9^{b}$
		1.235 <sup>c</sup>	$1.347^{c}$	$1.029^{c}$	$1.018^{c}$		113.9 <sup>c</sup>	$120.2^{c}$	116.9 <sup>c</sup>		$0.1^{c}$	179.8 <sup>c</sup>
lm.2	$0.983^{a}$	1.367 <sup>a</sup>	1.236 <sup>a</sup>	$1.027^{a}$		106.6 <sup>a</sup>	$112.0^{a}$	$106.2^{a}$		$0.0^{a}$		$180.0^{a}$
	$0.994^{b}$	$1.377^{b}$	$1.250^{b}$	$1.034^{b}$		$105.9^{b}$	$111.6^{b}$	$105.5^{b}$		$0.0^{b}$		$180.0^{b}$
	$0.997^{c}$	1.379 <sup>c</sup>	1.251 <sup>c</sup>	$1.037^{c}$		$105.7^{c}$	$111.5^{c}$	$105.4^{c}$		$0.0^{c}$		$180.0^{c}$
lm.3	$0.970^{a}$	1.393 <sup>a</sup>	$1.231^{a}$	$1.028^{a}$		103.0 <sup>a</sup>	109.5 <sup>a</sup>	104.9 <sup>a</sup>		$180.0^{a}$		$180.0^{a}$
	$0.978^{b}$	$1.410^{b}$	$1.243^{b}$	$1.035^{b}$		$101.9^{b}$	$109.0^{b}$	$104.1^{b}$		$180.0^{b}$		$180.0^{b}$
	0.981 <sup>c</sup>	1.413 <sup>c</sup>	$1.244^{c}$	1.038 <sup>c</sup>		$101.8^{c}$	$108.9^{c}$	$104.0^{c}$		$180.0^{c}$		$180.0^{c}$
lm.4	$0.983^{a}$	1.394 <sup>a</sup>	1.226 <sup>a</sup>	1.043 <sup>a</sup>		109.4 <sup>a</sup>	118.4 <sup>a</sup>	113.5 <sup>a</sup>		$0.0^{a}$		$0.0^{a}$
	$0.993^{b}$	$1.411^{b}$	$1.236^{b}$	$1.052^{b}$		$108.6^{b}$	$118.6^{b}$	113.6 <sup>b</sup>		$0.0^{b}$		$0.0^{b}$
	0.995 <sup>c</sup>	1.413 <sup>c</sup>	1.237 <sup>c</sup>	1.055 <sup>c</sup>		$108.5^{c}$	$118.6^{c}$	$113.5^{c}$		$0.0^{c}$		$0.0^{c}$
lm.5	0.971 <sup>a</sup>	$1.428^{a}$	$1.221^{a}$	1.039 <sup>a</sup>		103.8 <sup>a</sup>	112.4 <sup>a</sup>	111.5 <sup>a</sup>		$180.0^{a}$		$0.0^{a}$
	$0.979^{b}$	$1.452^{b}$	$1.229^{b}$	$1.048^{b}$		$102.7^{b}$	$112.5^{b}$	$111.9^{b}$		$180.0^{b}$		$0.0^{b}$
	0.981 <sup>c</sup>	1.455 <sup>c</sup>	1.231 <sup>c</sup>	$1.049^{c}$		$102.7^{c}$	$112.4^{c}$	$111.8^{c}$		$180.0^{c}$		$0.0^{c}$

<sup>a</sup> B3LYP. <sup>b</sup> PW91. <sup>c</sup> BP86.

TABLE 6: Structural Parameters (Å and deg) of Transition States in the Dissociation Reaction of NH<sub>2</sub>NO Calculated Using the B3LYP, PW91, and the BP86 Exchange–Correlation Functionals

	$\delta$ (H–O)	$\delta(O-N)$	$\delta(N-N)$	$\delta$ (N-H)	α(H-O-N)	α(O-N-N)	a(N-N-H)	a(H-O-N-N)	α(O-N-N-H)
ts.1	1.354 <sup>a</sup>	1.291 <sup>a</sup>	1.273 <sup>a</sup>	1.021 <sup>a</sup>	78.3 <sup>a</sup>	102.9 <sup>a</sup>	117.9 <sup>a</sup>	$0.0^{a}$	$180.0^{a}$
	$1.365^{b}$	$1.302^{b}$	$1.286^{b}$	$1.029^{b}$	$78.3^{b}$	$102.7^{b}$	$117.5^{b}$	$0.0^{b}$	$180.0^{b}$
	1.369 <sup>c</sup>	$1.303^{c}$	$1.288^{c}$	$1.031^{c}$	$78.4^{c}$	$102.8^{c}$	$117.4^{c}$	$0.0^{c}$	$180.0^{c}$
ts.2	$0.972^{a}$	$1.438^{a}$	$1.225^{a}$	$1.032^{a}$	$105.2^{a}$	$109.8^{a}$	$105.0^{a}$	$86.8^{a}$	$177.4^{a}$
	$0.979^{b}$	$1.460^{b}$	$1.235^{b}$	$1.041^{b}$	$104.2^{b}$	$109.2^{b}$	$104.3^{b}$	$87.0^{b}$	$177.2^{b}$
	$0.982^{c}$	1.463 <sup>c</sup>	$1.237^{c}$	1.043 <sup>c</sup>	$104.1^{c}$	$109.2^{c}$	$104.2^{c}$	$87.0^{c}$	$177.2^{c}$
ts.3	$0.979^{a}$	$1.484^{a}$	1.193 <sup>a</sup>	$0.998^{a}$	$105.9^{a}$	$114.8^{a}$	$178.1^{a}$	$0.0^{a}$	$180.0^{a}$
	$0.986^{b}$	$1.551^{b}$	$1.197^{b}$	$1.004^{b}$	$104.6^{b}$	$114.9^{b}$	$176.2^{b}$	$0.0^{b}$	$180.0^{b}$
	$0.989^{c}$	$1.551^{c}$	1.199 <sup>c</sup>	$1.006^{c}$	$104.5^{\circ}$	$114.8^{\circ}$	$176.2^{\circ}$	$0.0^c$	$180.0^{c}$
ts.4	$0.973^{a}$	1.469 <sup>a</sup>	$1.217^{a}$	$1.040^{a}$	$105.7^{a}$	$114.8^{a}$	$112.7^{a}$	$67.7^{a}$	$-0.1^{a}$
	$0.981^{b}$	$1.508^{b}$	$1.223^{b}$	$1.048^{b}$	$104.0^{b}$	$114.1^{b}$	$113.0^{b}$	$70.8^{b}$	$-0.2^{b}$
	$0.983^{c}$	$1.510^{\circ}$	$1.224^{c}$	$1.051^{c}$	$104.0^{c}$	$114.0^{c}$	$112.9^{c}$	$70.5^{c}$	$-0.2^{c}$
ts.5	$0.972^{a}$	$1.551^{a}$	$1.178^{a}$	$0.997^{a}$	$101.5^{a}$	110.9 <sup>a</sup>	$174.3^{a}$	$180.0^{a}$	$180.0^{a}$
	$0.981^{b}$	$1.613^{b}$	$1.184^{b}$	$1.024^{b}$	$99.9^{b}$	$110.8^{b}$	$172.5^{b}$	$180.0^{b}$	$180.0^{b}$
	$0.982^{c}$	1.613 <sup>c</sup>	$1.186^{c}$	$1.004^{c}$	99.9 <sup>c</sup>	$110.8^{c}$	$172.6^{\circ}$	$180.0^{c}$	$180.0^{c}$
ts.6	$0.973^{a}$	$1.850^{a}$	1.164 <sup>a</sup>	1.136 <sup>a</sup>	$141.7^{a}$	$88.9^{a}$	$104.4^{a}$	$180.0^{a}$	$0.0^a$
	$0.983^{b}$	$1.924^{b}$	$1.170^{b}$	$1.140^{b}$	$139.5^{b}$	$88.8^{b}$	$103.3^{b}$	$180.0^{b}$	$0.0^b$
	$0.984^{c}$	$1.924^{c}$	$1.171^{c}$	$1.120^{c}$	139.5 <sup>c</sup>	$88.8^{c}$	$103.4^{\circ}$	$180.0^{c}$	$0.0^c$
ts.7	$1.450^{a}$	$1.250^{a}$	$1.183^{a}$	$1.466^{a}$	$89.2^{a}$	$127.6^{a}$	$92.2^{a}$	$0.0^{a}$	$0.0^{a}$
	$1.475^{b}$	$1.254^{b}$	$1.198^{b}$	$1.442^{b}$	$88.8^{b}$	$127.6^{b}$	$93.0^{b}$	$0.0^{b}$	$0.0^{b}$
	$1.478^{c}$	$1.256^{c}$	$1.199^{c}$	$1.450^{\circ}$	$88.1^{c}$	$127.1^{c}$	$92.9^{c}$	$0.0^c$	$0.0^c$

<sup>a</sup> B3LYP. <sup>b</sup> PW91. <sup>c</sup> BP86.

TABLE 7: Relative Energies (kcal/mol) of Intermediates and Transition States in the Dissociation Reaction of NH<sub>2</sub>NO Calculated Using the B3LYP, PW91, and the BP86 Exchange–Correlation Functionals

	B3LYP	B3LYP-ZPEC <sup>a</sup>	PW91	PW91-ZPEC <sup>a</sup>	BP86	BP86-ZPEC <sup>a</sup>
NH <sub>2</sub> NO	0.00	0.00	0.00	0.00	0.00	0.00
lm.2	2.85	2.33	3.75	3.28	3.41	2.94
lm.3	3.67	3.07	4.67	4.08	4.41	3.81
lm.4	10.08	10.42	10.09	10.53	9.68	10.11
lm.5	3.03	2.99	3.49	3.51	3.11	3.13
ts.1	32.30	35.04	27.95	30.63	27.29	29.94
ts.2	12.54	13.11	14.49	15.12	14.15	14.76
ts.3	38.93	41.31	36.76	39.36	36.34	38.91
ts.4	13.34	14.38	14.17	15.31	13.73	14.86
ts.5	35.66	37.87	33.25	35.52	32.90	35.14
ts.6	24.20	29.77	22.12	27.54	21.10	26.62
ts.7	50.85	56.11	43.31	48.24	42.26	47.33
$N_2 + H_2O$	-62.47	-66.05	-55.47	-58.79	-54.17	-57.46
$N_2O + H_2$	10.96	3.85	6.36	0.36	7.90	1.21

<sup>a</sup> Including the zero-point vibrational energies correction.

## **IV.** Conclusion

Quantum chemical calculations carried out on a V<sub>2</sub>O<sub>9</sub>H model cluster support earlier experimental findings which indicated that the vanadium oxide-catalyzed SCR of NO is initiated by NH<sub>3</sub> adsorption on a Brønsted acid site. The adsorbed NH<sub>3</sub> is activated by transferring an H to the V<sup>5+</sup>=O site, which becomes partly reduced. Gaseous or weakly adsorbed NO subsequently reacts with this activated NH<sub>3</sub>, leading to the formation of V<sup>4+</sup>–OH and NH<sub>2</sub>NO. The NH<sub>2</sub>NO species is not observed experimentally under SCR conditions, because it undergoes rapid decomposition, yielding the reaction products N<sub>2</sub> and H<sub>2</sub>O. In order to complete the catalytic cycle, V<sup>4+</sup>– OH must be oxidized to V<sup>5+</sup>=O. The theoretical findings that

TABLE 8: Vibrational Frequencies (cm<sup>-1</sup>) of Intermediates in the Dissociation Reaction of NH<sub>2</sub>NO Calculated using the B3LYP, PW91, and the BP86 Exchange–Correlation Functionals

	$\omega_1$	$\omega_2$	$\omega_3$	$\omega_4$	$\omega_5$	$\omega_6$	$\omega_7$	$\omega_8$	$\omega_9$
$lm.1^d$	242 <sup>a</sup>	628 <sup>a</sup>	712 <sup>a</sup>	1110 <sup>a</sup>	1226 <sup>a</sup>	1581 <sup>a</sup>	1606 <sup>a</sup>	3472 <sup>a</sup>	3710 <sup>a</sup>
	$241^{b}$	594 <sup>b</sup>	701 <sup>b</sup>	$1039^{b}$	$1177^{b}$	$1523^{b}$	1546 <sup>b</sup>	3366 <sup>b</sup>	3623 <sup>b</sup>
	$235^{c}$	$592^{c}$	699 <sup>c</sup>	1033 <sup>c</sup>	$1173^{c}$	1515 <sup>c</sup>	1537 <sup>c</sup>	$3342^{c}$	3601 <sup>c</sup>
$lm.2^{e}$	653 <sup>a</sup>	$665^{a}$	944 <sup>a</sup>	957 <sup>a</sup>	1361 <sup>a</sup>	1435 <sup>a</sup>	$1647^{a}$	$3428^{a}$	3565 <sup>a</sup>
	$638^{b}$	$662^{b}$	906 <sup>b</sup>	$909^{b}$	1309 <sup>b</sup>	1390 <sup>b</sup>	$1567^{b}$	3339 <sup>b</sup>	3415 <sup>b</sup>
	636 <sup>c</sup>	661 <sup>c</sup>	901 <sup>c</sup>	905 <sup>c</sup>	1303 <sup>c</sup>	1383 <sup>c</sup>	1559 <sup>c</sup>	3317 <sup>c</sup>	3388 <sup>c</sup>
lm.3 <sup>e</sup>	507 <sup>a</sup>	665 <sup>a</sup>	911 <sup>a</sup>	965 <sup>a</sup>	$1328^{a}$	$1437^{a}$	$1689^{a}$	3416 <sup>a</sup>	3789 <sup>a</sup>
	$516^{b}$	$638^{b}$	$855^{b}$	927 <sup>b</sup>	$1279^{b}$	1391 <sup>b</sup>	$1610^{b}$	3330 <sup>b</sup>	3677 <sup>b</sup>
	513 <sup>c</sup>	636 <sup>c</sup>	$850^{c}$	923 <sup>c</sup>	$1273^{c}$	$1385^{c}$	$1602^{c}$	3308 <sup>c</sup>	3656 <sup>c</sup>
<b>lm.</b> 4 <sup>e</sup>	$488^{a}$	649 <sup>a</sup>	$870^{a}$	957 <sup>a</sup>	$1279^{a}$	$1404^{a}$	1683 <sup>a</sup>	3166 <sup>a</sup>	3557 <sup>a</sup>
	$509^{b}$	$600^{b}$	$809^{b}$	$922^{b}$	$1229^{b}$	1340 <sup>b</sup>	$1615^{b}$	3061 <sup>b</sup>	3420 <sup>b</sup>
	$508^{c}$	599 <sup>c</sup>	806 <sup>c</sup>	917 <sup>c</sup>	$1223^{c}$	$1334^{c}$	$1607^{c}$	$3034^{c}$	3393 <sup>c</sup>
lm.5 <sup>e</sup>	463 <sup>a</sup>	613 <sup>a</sup>	803 <sup>a</sup>	$1008^{a}$	$1280^{a}$	1386 <sup>a</sup>	$1729^{a}$	3256 <sup>a</sup>	3782 <sup>a</sup>
	$472^{b}$	$569^{b}$	$740^{b}$	$968^{b}$	$1225^{b}$	1319 <sup>b</sup>	$1664^{b}$	3164 <sup>b</sup>	3673 <sup>t</sup>
	467 <sup>c</sup>	567 <sup>c</sup>	736 <sup>c</sup>	964 <sup>c</sup>	$1217^{c}$	1313 <sup>c</sup>	$1657^{c}$	$3138^{c}$	3650

<sup>*a*</sup> B3LYP. <sup>*b*</sup> PW91. <sup>*c*</sup> BP86. <sup>*d*</sup>  $\omega_1$ ,  $\gamma$ (NH<sub>2</sub>);  $\omega_2$ ,  $\rho$ (NH<sub>2</sub>);  $\omega_4$ ,  $\nu$ (NN);  $\omega_5$ ,  $\rho$ (NH<sub>2</sub>);  $\omega_6$ ,  $\delta$ (NH<sub>2</sub>);  $\omega_7$ ,  $\nu$ (NO);  $\omega_8$ ,  $\nu_{sym}$ (NH);  $\omega_9$ ,  $\nu_{asym}$ (NH). <sup>*e*</sup>  $\omega_4$ ,  $\nu$ (NO);  $\omega_7$ ,  $\nu$ (NN);  $\omega_8$ ,  $\nu$ (NH);  $\omega_9$ ,  $\nu$ (OH).

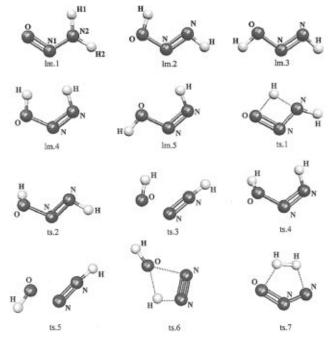


Figure 9. Structures of several intermediates and transition states in the dissociation reaction of  $NH_2NO$ .

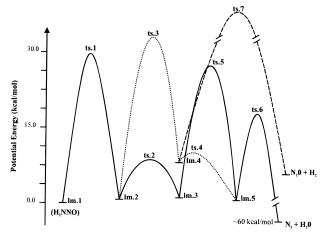


Figure 10. Relative energies of intermediates and transition states in the dissociation reaction of  $NH_2NO$ .

emerged from our DFT modeling of the SCR reaction are in agreement with an Eley–Rideal-type mechanism. They provide a detailed analysis of the energetical and structural characteristics of the reaction between activated  $NH_3$  and NO.

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#### **References and Notes**

(1) Bosch, H.; Janssen, F. Catal. Today **1987**, 2 (4), 369. Bond, G. C.; Tahir, S. F. Appl. Catal. **1991**, 71 (1).

- (2) Takagi, M.; Kawai, T.; Soma, M.; Onishi, T.; Tamuru, T. J. Catal. 1977, 50, 441.
- (3) Inomata, M.; Miyamoto, A.; Murakami, Y. J. Catal. 1980, 62, 140.
  (4) Gasior, M.; Haber, J.; Machej, T.; Czeppe, T. J. Mol. Catal. 1988, 43, 359.
- (5) Rajadhyaksha, R. A.; Knözinger, H. Appl. Catal. 1989, 51, 81.
- (6) Odriozola, J. A.; Heineman, H.; Somorjai, G. A.; De la Banda, J. F.; Pereira, P. *Appl. Catal.* **1989**, *119*, 71.
- (7) Ramis, G.; Busca, G.; Lorenzelli, V.; Forzatti, P. Appl. Catal. 1990, 64, 243.
  - (8) Schraml, M.; Wokaum, A.; Baiker, A. J. Catal. 1990, 124, 86.
    (9) Topsøe, N. Y. J. Catal. 1991, 128, 499.
- (10) Went, G. T.; Leu, L.-J.; Rosin, R. R.; Bell, A. T. J. Catal. 1992, 134, 492.

(11) Dumesic, J. A. In *New Frontiers in Catalysis*, Proceedings of the 10th International Congress on Catalysis, Budapest, Hungary; Guczi, L., *et al.*, Eds.; Akadémiai Kadó: Budapest, 1993; p 1325.

(12) Schneider, H.; Tschudin, S.; Schneider, M.; Wokaun, A.; Baiker, A. J. Catal. **1994**, 147, 5.

- (13) Ramis, G.; Busca, G.; Lorenzelli, V.; Forzatti, P. Appl. Catal. 1990, 64, 259.
- (14) Takagi, M.; Kawai, T.; Soma, M.; Onishi, T.; Tamuru, T. J. Phys. Chem. 1976, 80, 430.
- (15) Janssen, F. J. J. G.; van den Kerkhof, F. M. G.; Bosch, H.; Ross, J. R. H. J. Phys. Chem. **1987**, *91*, 5921.
- (16) Topsøe, N.-Y.; Topsøe, H. Catal. Today 1991, 9, 77. Topsøe, N.-Y. Science 1994, 265, 1217.
- (17) Schneider, H.; Tschudin, S.; Schneider, M.; Wokaum, A.; Baiker, A. J. Catal. **1994**, 147, 5.
- (18) Topsøe, N.-Y.; Salbiak, T.; Clausen, S. B.; Srnak, T. Z.; Dumesic, J. A. J. Catal. **1992**, *134*, 742.

(19) Srnak, T. Z.; Dumesic, J. A.; Clausen, B. S.; Törnqvist, E.; Topsøe, N.-Y. J. Catal. 1992, 135, 246.

- (20) Baltensperger, U.; Amman, M.; Bochert, U.; Eichler, B.; Gäggeler, H. W.; Jost, D.; Kovacs, J.; Türler, A.; Scherer, U. W.; Baiker, A. J. Phys. Chem. **1995**, 97, 12325.
  - (21) Duan, X.; Page, M. J. Mol. Struct. (THEOCHEM) 1995, 333, 233.
  - (22) Kulkarni, S. A.; Pundnik, S. S. Chem. Phys. Lett. 1995, 245, 143.
  - (23) Diau, E. R.-W.; Smith, S. C. J. Phys. Chem. 1996, 100, 12349.
  - (24) Walch, S. P. J. Chem. Phys. 1993, 99(7), 5295.

(25) Bradley, K. S.; McCabe, P.; Schatz, G. C.; Walch, S. P. J. Chem. Phys. **1995**, 102(17), 6696.

(26) Koizumi, H.; Schatz, G. C.; Walch, S. P. J. Chem. Phys. **1991**, 95, 4130.

(27) Wolf, M.; Yang, D. L.; Durant, J. L. J. Photochem. Photobiol. A: Chem. 1994, 80, 85.

(28) Durant, J. L., Jr. In *Reactions of NHx Species, Research in Chemical Kinetics, Vol. 3*; Compton, R. G., Hancock, G., Eds.; Elsevier Science B.V.: Amsterdam, 995; pp 69–115.

(29) Melius, C. F.; Binkley, J. S. Symp. (Int.) Combust. Proc. 1984, 20, 575.

(30) Casewit, C. J.; Goddard, W. A. J. Am. Chem. Soc. 1982, 104, 3280.
(31) Abou-Rachid, H.; Pouchan, C.; Chaillet, M. Chem. Phys. 1984, 90, 243.

(32) Harrison, J. A.; Maclagan, G. A. R.; White, A. R. J. Phys. Chem. 1987, 91, 6683

- (33) Gilardoni, F.; Weber, J.; Baiker, A. Int. J. Quantum Chem. 1997, 61, 683-688.
  - (34) Witko, M.; Hermann, K. J. Mol. Catal. 1993, 81, 279.
  - (35) Hermann, K.; Bagus, P. S. Phys. Rev. 1978, B17, 4082.
  - (36) Witko, M.; Tokarz, R.; Haber, J. J. Mol. Catal. 1991, 66, 205.
- (37) Petelenz, P.; Broclawik, E. J. Mol. Catal. 1991, 68, 223; Ibid. 1993, 80, 341.
- (38) Nalewajjski, R. F. J. Mol. Catal. 1993, 82, 371.
- (39) Kobayashi, H.; Yamaguchi, M.; Tanaka, T.; Nishimura, Y.; Kawakami, Y. H.; Yoshida, S. J. Phys. Chem. 1988, 92, 2516.

(40) Efstathiou, A. M.; Fliatoura, K. Appl. Catal., B 1995, 6

- (41) Andzelm, J.; Radzio, E.; Salahub, D. R. J. Chem. Phys. 1985, 83, 4573.
- (42) Salahub, D. R. In Applied Quantum Chemistry; Smith, V. H., Schafer, H. F., Morokuma, K., Eds.; Reidel: Dordrecht, 1986; p 185.

- (43) Salahub, D. R. Adv. Chem. Phys. 1987, 69, 447.
- (44) Salahub, D. R.; Fournier, R.; Mlynarski, P.; Papai, I.; St-Amant,
- A.; Ushio, J. In Density Functional Methods in Chemistry; Labanowski,
- K., Andzelm, J., Eds.; Springer: New York, 1991; p 77. (45) Becke, A. D. J. Chem. Phys. 1988, 88, 2457. Becke, A. D. Phys.
- Rev. A. 1988, 38, 3098.
  - (46) Perdew, J. P. Phys. Rev. B 1986, 33, 8822; 1986, 34, 7046.
- (47) Godbout, N.; Salahub, D. R.; Andzelm, J.; Wimmer, E. Can. J. Chem. 1992, 70, 560.
- (48) Frisch, M. J.; Trucks, G. W.; Schlegel, H. B.; Gill, P. M. W.; Johnson, B. G.; Wong, M. W.; Foresman, J. B.; Robb, M. A.; Head-Gordon,

- M.; Replogle, E. S.; Gomperts, R.; Andres, J. L.; Raghavachari, K.; Binkley, J. S.; Gonzales, C.; Martin, R. L.; Fox, D. J.; Defrees, D. J.; Baker, J.; Stewart, J. P. P.; Pople, J. A. Gaussian 94/DFT, revision F4; Gaussian,
- Inc.: Pittsburgh, PA 1995. (49) Becke, A. D. J. Chem. Phys. 1993, 98, 5648.
  - (50) Lee, C.; Yang, W.; Parr, R. G. Phys. Rev. B 1988, 37, 785.
  - (51) Miehlich, B.; Savin, A.; Stoll, H.; Preuss, H. Chem. Phys. Lett.
- 1989, 157, 200. (52) Perdew, J. P.; Wang, Y. Phys. Rev. 1992, B45, 13244.
  - (53) Rauhut, G.; Pulay, P. J. Phys. Chem. 1995, 99, 3093.
- (54) Zhou, X.; Wheeless, C. J. M.; Liu, R. Vib. Spectrosc. 1996, 12, 53-63.
  - (55) Wong, M. W. Chem. Phys. Lett. 1996, 256, 391-399.
  - (56) Farber, M.; Harris, S. P. J. Chem. Phys. 1984, 88, 680.
- (57) Duffy, B. L.; Curry-Hyde, H. E.; Cant, N. W.; Nelson, P. F. Catal. Lett. 1994, 28, 167.
- (58) Topsøe, N.-Y.; Topsøe, H.; Dumesic, J. J. Catal. 1995, 151, 226. (59) Topsøe, N.-Y.; Topsøe, H.; Dumesic, J. J. Catal. 1995, 151, 241.
- (60) Adams, R. C.; Xu, L.; Moller, K.; Bein, T.; Delgass, W. N. Catal.
- Today 1997, 33, 263-278. (61) Pople, J. A.; Scott, A. P.; Wong, M. W.; Israel, L. R. J. Chem. 1993, 33, 345.
- (62) Hout, R. F.; Levi, B. A.; Hehre, W. J. J. Comput. Chem. 1982, 3, 234.
- (63) DeFrees, D. J.; McLean, A. D. J. Chem. Phys. 1985, 82, 333.
- (64) Latajka, Z.; Bouteiller, Y. J. Chem. Phys. 1994, 101, 119.